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How to solve slopes of parallel and perpendicular lines

How to use Algebra to find parallel and perpendicular lines. Parallel Lines How do we know when two lines are parallel? Their slopes are the same! The slope is the value m in the equation of a line: y = mx + b Example: Find the equation of the line that is: parallel to y = 2x + 1 and passes though the point (5,4) The slope of y = 2x + 1 is: 2 The parallel line needs to have the same slope of 2. We can solve it using the "point-slope" equation of a line: y - y1 = 2(x - x1) And then put in the point (5,4): y - 4 = 2(x - 5) And that answer is OK, but let's also put it in y = mx + b form: y - 4 = 2x - 10 y = 2x - 6 Vertical Lines But this does not work for vertical lines ... I explain why at the end. Not The Same Line Be careful! They may be the same line (but with a different equation), and so are not parallel. How do we know if they are really the same line? Check their y-intercept is 2 For y - 2 = 3x: the slope is 3, and y-intercept is 2 In fact they are the same line and so are not parallel Perpendicular Lines Two lines are Perpendicular to y = -4x + 10 and passes though the point (7,2) The slope of y=-4x+10 is: -4 The negative reciprocal of that slope is: m=-1-4=14 So the perpendicular line will have a slope of 1/4: $y-y_1=(1/4)(x-x_1)$ And now put in the point (7,2): $y-2=(1/4)(x-x_1)$ And $y=x_1$ and $y=x_2$ and $y=x_2$ and $y=x_1$ and $y=x_2$ and $y=x_1$ and $y=x_2$ and $y=x_1$ and $y=x_2$ and $y=x_2$ and $y=x_2$ and $y=x_1$ and $y=x_2$ and $y=x_2$ and $y=x_1$ and $y=x_2$ Perpendicular When we multiply a slope m by its perpendicular? Line Slope y = 2x + 1 2 y = -0.5x + 4 y = -0.5 When we multiply the two slopes we get: $2 \times (-0.5) = -1$ Yes, we got -1, so they are perpendicular. Vertical Lines The previous methods work nicely except for a vertical line is parallel to another vertical line is parallel to another vertical line. a vertical line is perpendicular to a horizontal line (and vice versa). Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines WTAMU > Virtual Math Lab > College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright © 2017 MathsIsFun.com College Algebra Tutorial 28: Parallel and Perpendicular Lines wto Summary parallel lines: same slope (-1/m) Copyright (-1/m) C parallel to a given line. Find the slope of a line that is perpendicular to a given line. Introduction This tutorial looks at the relationship between the slope of a line given an equation and how to write the equation of a line. If you need a review on these concepts, feel free to go to Tutorial 26: Equations of Lines. Let's see what you can do with parallel lines are equal. Note that two lines are parallel if their slopes are equal and they have different y-intercepts. Perpendicular Lines and Their Slopes In other words, perpendicular slopes are negative reciprocals of each other. Here is a quick review on how to use this form, feel free to go to Tutorial 26: Equations of Lines. Slope/Intercept Equation of a Line If your linear equation is written in this form, m represents the slope and b represents the y-intercept. This form can be handy if you need to find the slope of a line given the equation. Example 1: Find the slope of any line that is a) parallel and b) perpendicular to the line. Before we tackle finding the parallel and perpendicular slopes it really can help us out if we find the slope of the given line. Recall that when you are given the equation of a line that you can find the slope of it by writing it in the slope/intercept form, , where m is the slope and b is the y-intercept of the line. This equation is already written in the slope/intercept form: *Written in slope/intercept form Lining up the form with the equation we have been given, can you see what the slope of the parallel line: Since parallel line to this line is going to be? Pat yourself on the back if you said -7. Slope of the perpendicular line: Since the slopes of perpendicular line are negative reciprocals of each other, what do you think the slope of any perpendicular line to this line is? Give yourself a high five if you said 1/7. Remember that you take the reciprocal which is -1/7 and then you negate it to get the 1/7 for your perpendicular slope. The slope of any parallel line to the line is -7 and the slope of any perpendicular line to the line is 1/7. Example 2: Find the slope of the line that is a) parallel and perpendicular slopes it really can help us out if we find the slope of the given line. Recall that when you are given the equation of a line that you can find the slope of it by writing it in the slope/intercept form, , where m is the slope and b is the y-intercept form with the equation we get: *Inverse of sub. 2/3x is add. 2 correct!!! Slope of the parallel line: Since parallel line: Since the slope of the parallel line is going to be? Pat yourself on the back if you said 2/3. Slope of the perpendicular line: Since the slopes of perpendicular line is? Give yourself a high five if you said -3/2. Remember that you take the reciprocal which is 3/2 and then you negate it to get the -3/2 for your perpendicular line is -3/2. Example 3: Find the slope of the line that is a) parallel and b) perpendicular to the line. Do you remember what special type of line this equation is? It is a vertical line. If you need a review on vertical line is line is line is line. Since parallel line is have the same slope, what do you think the slope of the parallel line is line. going to be? Pat yourself on the back if you said undefined. Slope of the perpendicular line: Since slopes of perpendicular line is? This one is a little trickier. Vertical lines are perpendicular to each other, what do you think the slope of the perpendicular line is? line in this case would be the slope of the perpendicular line is 0. Example 4: Find the slope of the perpendicular line is 0. Example 4: Find the slope of the perpendicular line is 0. review on horizontal lines, feel free to go to Tutorial 27: Graphing Lines. What is the slope of the parallel line: Since parallel line is going to be? Pat yourself on the back if you said 0. Slope of the perpendicular line: Since slopes of perpendicular lines are negative reciprocals of each other, what do you think the slope of the perpendicular line is? This one is a little trickier. Vertical lines are perpendicular to each other, what do you think the slope of the perpendicular line is? This one is a little trickier. Vertical lines are perpendicular lines are per parallel line is 0 and the slope of the perpendicular line is undefined. Here is a quick review on how to use this form, feel free to go to Tutorial 26: Equations of Lines Point/Slope Form of an Equation A line going through the point and having slope of m would have the equation We can use this form to plug into when we need to come up with a linear equation. When writing an equation of a line, keep in mind that you ALWAYS need two pieces of information, you plug the x and y values from your point and the slope (m) value into the point/slope formula. Example 5: Write an equation for the line in point/slope form and slope/intercept form that passes through (-2, -5) and parallel to the line and the slope, you are correct. We have a point, however what about the slope? Does this mean we can't work out the problem? You are not going to get off that easily. We need to do a little digging to get our slope. As mentioned above, parallel lines have the same slope. So, if we know the slope of the line parallel to our line, we have it made. Let's find the slope of the given line: *Slope/intercept form of the line Now keep in mind that this is not the equation of our line but of a line parallel to our line. We needed to write it this way so we could get the slope of 4. OK, now we have our slope, which is 4. Now it is just like problems in Tutorial 26: Equations of Lines, we put the slope and one point into the point/slope equation. Point/slope form of the line Make sure that you are careful when one of your values is negative and you have to subtract it as we did in line 2. y - (-2) is not the same as x - 2. Next, we want to write it in the Slope/Intercept Form, which basically means we need to solve for y: *Dist. the 4 through (-2, -5) and is parallel to the line is y + 5 = 4(x + 2) OR y = 4x + 3. Example 6: Write an equation for the line in point/slope form and slope/intercept form that passes through (3, 2) and perpendicular to the line. What are the two things we need to write an equation of a line???? If you said any point on the line and the slope, you are correct. We have a point, however what about the slope? Does this mean we can't work out the problem? You are not going to get off that easily. We need to do a little digging to get our slope. As mentioned above, the slopes of perpendicular lines are negative reciprocals of each other. So, if we know the slope of a line perpendicular to our line, we have it made. Let's find the slope of the given line: *Inverse of add. 2x is sub. 2x *Inverse of mult. by -5 *Slope/intercept form of the line Now keep in mind that this is not the equation of our line but of the line parallel to our line. We needed to write it this way so we could get the slope of -5/2 (the negative reciprocal of 2/5). OK, now we have our slope, which is -5/2. Now it is just like problems in Tutorial 26: Equations of Lines, we put the slope and one point into the point/slope form. *Point/slope form of the line Next, we want to write it in the Slope/Intercept Form, which basically means we need to solve for y: *Dist. the -5/2 through () *Inverse of sub. 2 is add. 2 *Slope/intercept Form. form of the line The equation of the line that passes through (3, 2) and perpendicular to the line is y - 2 = -5/2(x - 3) OR y = -5/2x + 19/2. Practice Problems These are practice problems to help bring you to the next level. It will allow you to check and see if you have an understanding of these types of problems. Math works just like anything else, if you want to get good at it, then you need to practice, to get good at their sport or instrument. In fact there is no such thing as too much practice, practic your answer by clicking on the link for the answer/discussion for that problem. At the link you will find the answer as well as any steps that went into finding that answer/discussion to 1a) 1b. (answer/discussion to 1b) 1c. (answer/discussion to 1c) Practice Problems 2a - 2b: Write an equation for the line in point/slope form and slope/intercept form that has the given condition. 2a. Passes through (-7, 2) and is parallel to . (answer/discussion to 2a) Need Extra Help on these Topics? WTAMU > Virtual Math Lab > College Algebra Last revised on Feb. 20, 2010 by Kim Seward. 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